

## Homework 8 (due Apr 8)

Consider a beam of emittance  $\varepsilon = 10 \mu\text{m}$  propagating in a periodic FODO structure consisting of thin lenses of focal lengths  $\pm F = \pm 8 \text{ m}$  separated by drifts of length  $L = 10 \text{ m}$ .

1. Write the transfer matrix  $M$  for one FODO period and calculate the phase advance  $\mu$ . Is the motion stable?
2. Compare the transfer matrix  $M$  expressed in terms of  $F$  and  $L$  with the one expressed in terms of the Courant-Snyder parameters to calculate the values of  $\alpha$ ,  $\beta$ , and  $\gamma$  at two locations: (1) just before the focusing lenses and (2) just before the defocusing lenses.
3. Use the propagation matrix for the Courant-Snyder parameters to produce a plot of  $\alpha(s)$ ,  $\beta(s)$ , and  $\gamma(s)$  in the interval  $0 \text{ m} < s < 40 \text{ m}$ .
4. On a separate plot, draw the beam envelope  $\sqrt{\varepsilon\beta(s)}$  for  $0 \text{ m} < s < 40 \text{ m}$ .